

**Exercise 1** *Step-size controlled solution of the Curtiss–Hirschfelder equation*

The code for this problem can be found in `obelix:~wdobler/Phys535/idl/Curtiss-Hirschfelder`

- (a) Numerically solve the Curtiss–Hirschfelder equation for at least  $t = 50$ .
- (b) Adapt ‘`run.pro`’ to make it overplot minimum and maximum of  $\delta t$  instead of the average.
- (c) Find the largest error tolerance *err* that is acceptable (decision based on the two curves).
- (d) Add a third panel showing the difference between the numerical solution and  $\cos t$ . Compare with exact result, and find again the largest acceptable value of *err*.

**Exercise 2** *Van der Pol equation*

Now “vectorize” the files from the Curtiss–Hirschfelder experiments and use them to solve the van der Pol equations

$$\ddot{y} = -y + \mu(1 - y^2)\dot{y} \tag{1}$$

for  $\mu = 5$ .

Note: It is best to start with a full copy of the Curtiss–Hirschfelder directory.

- (a) Write Eq. (1) as a system of two first-order equations.
- (b) Now adapt the files `start.pro`, `pde.pro`, `run.pro`, and ‘`print.pro`’ to make them work with a 2-element array `f`.
- (c) Adapt ‘`README`’, so you can still use this setup in a year from now...
- (d) Plot  $y(t)$ ,  $\dot{y}(t)$ ,  $\dot{y}(y)$ , and  $\delta t(t)$ .
- (e) How does the parameter  $\mu$  affect the behaviour of the time step  $\delta t(t)$ ?