

High-Energy Neutrinos Produced Interactions of Relativistic Protons in Shocked Pulsar Winds

ApJ, 600, 883-904 (2004).

S. Nagataki (Kyoto University)

Ultra Relativistic Jets in Astrophysics
Bannff, Canada, July 13, 2005

§ Introduction

Previous Works

Gunn and Ostriker (1969) pointed out the possibility that a rotating magnetic neutron star may be a source of high energy cosmic rays.

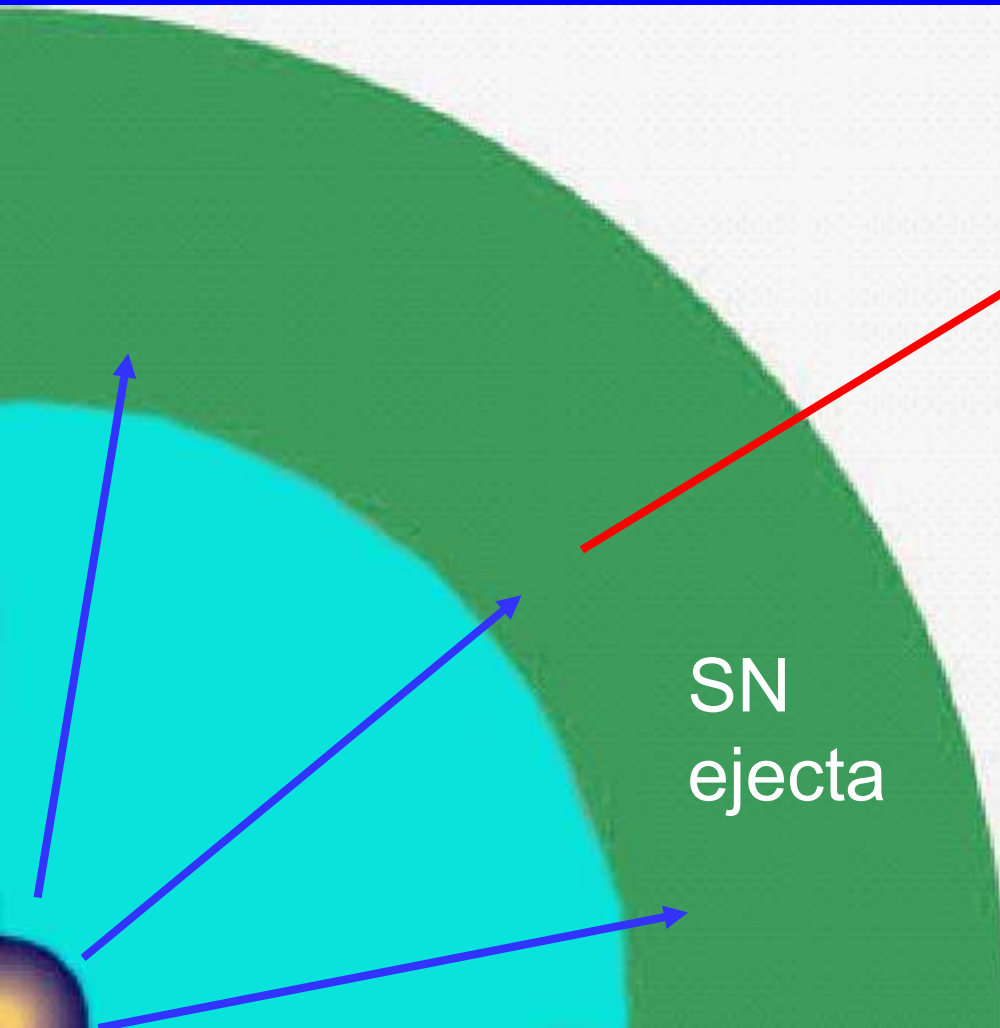
It is pointed out that **hadronic component may exist** in pulsar winds to satisfy the Goldreich-Julian value in the outflow (ex. Hoshino et al. 1992).

Moreover, **hadronic components** may be the **energetically dominant** species although they are dominated by electron-positron pairs in number, because inertial masses of hadrons are much larger than that of electrons (Hoshino et al. 1992).

Based on this assumption that hadronic components are not negligible in pulsar winds, some scenarios are proposed to produce high energy neutrinos and gamma-rays generated through interactions between accelerated **high energy cosmic rays** and **surrounding photon fields** (Beal & Bednarek 2002) and/or **matter** (Protheroe et al. 1998; Bednarek and Bartosik 2003; Amato et al. 2003).

Location where neutrinos are produced

Blew arrow: neutron
Red arrow: neutrino



Iron is ejected from the
Surface of the neutron star.



Neutron is extracted by
photodisintegration of iron.



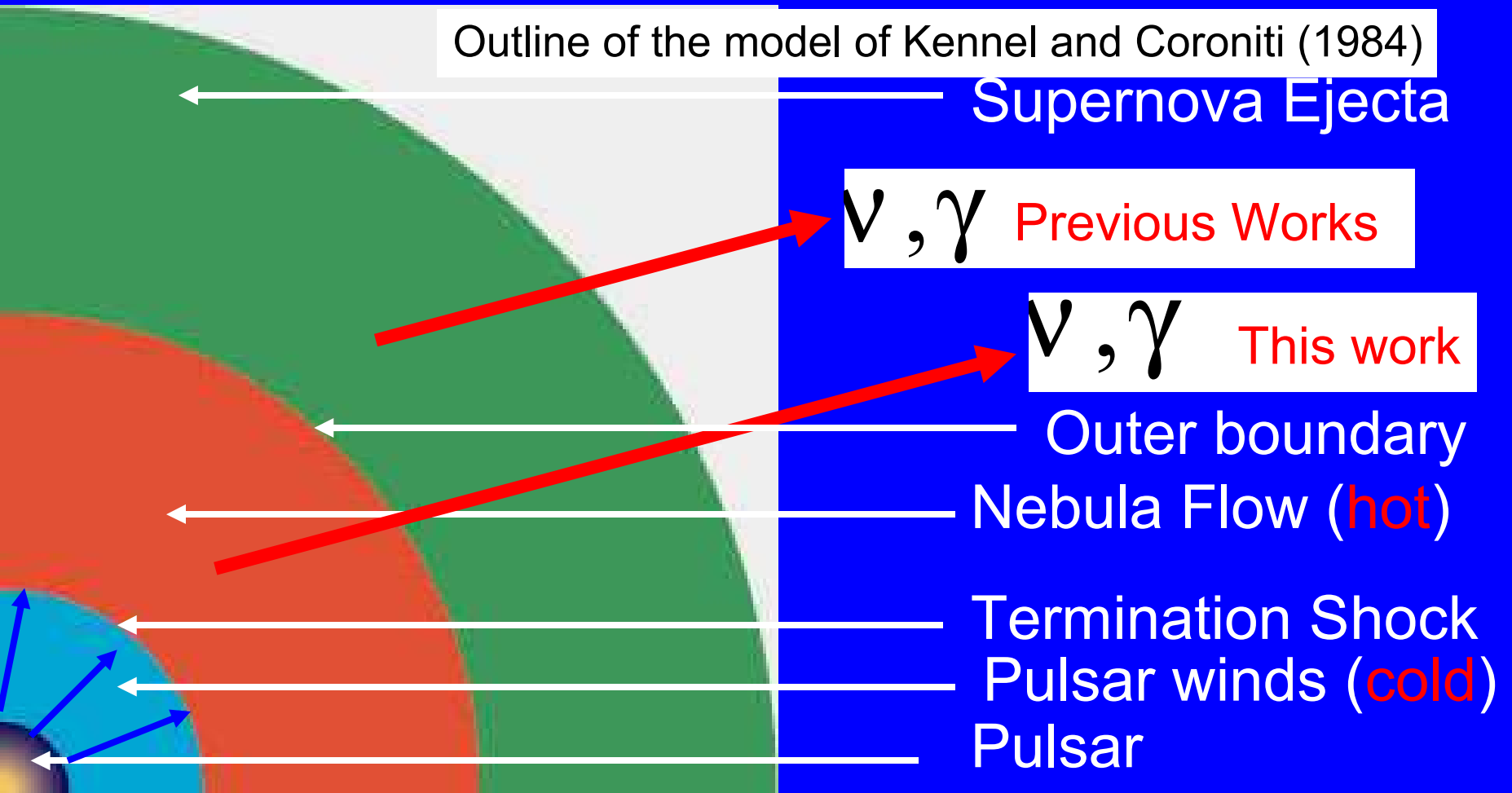
Neutron will interact
with supernova ejecta.

Dynamics of charged
particles are neglected.

Protheroe et al. 98

What's new?

In this work, we estimate fluxes of neutrinos and gamma-rays including an effect that has not been taken into consideration, that is, **interactions between high energy cosmic rays themselves** in the nebula flow, which is based on the model presented by Kennel and Coroniti (1984).



Assumptions in This Work

In this study, we consider the case where proton is the energetically dominant component ($n_p / (n_{e^+} + n_{e^-}) > 10^{-3}$).

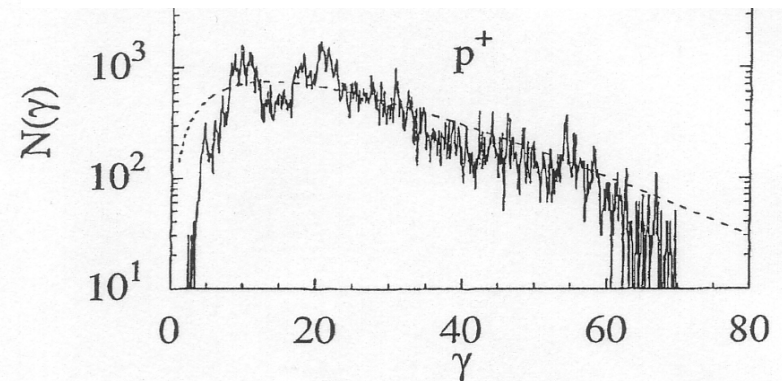
Initial bulk Lorentz factor of protons is constant and same with that of electrons.

Bulk flow is entirely **randomized** by passing through the termination shock and distribution functions of protons and electrons behind the termination shock obey the relativistic Maxwellians. This assumption is used in our calculations by Hoshino et al. 1992.

Energy distribution of protons behind the termination shock (Hoshino et al. 1992)

$$T_{p,2} / \gamma_1 m_p c^2 \approx 0.34$$

It is noted that the system is not thermalized but just randomized.



Contribution of Fermi I acceleration is not included in this study in order to avoid the uncertainty of the efficiency of the Fermi I acceleration.

§ Formulation

Procedure to Estimate Fluxes of Neutrinos and Gamma-rays

1. Hydrodynamics (Kennel & Coroniti 1984)

a. Pulsar Winds (with Monotonic Bulk Lorentz Factor)

b. Shock Conditions

Location of the termination shock is determined from the outer boundary conditions.

c. Nebula Flow

d. Outer boundary (SN ejecta)

2. Microphysics of proton-proton Interaction

Hydrodynamics (1)

Pulsar Winds (we determine the luminosity and bulk Lorentz factor of the wind as functions of B and P)

$$L = 9.6 \times 10^{42} \left(\frac{B_p}{10^{12} \text{G}} \right)^2 \left(\frac{R}{10^6 \text{cm}} \right)^6 \left(\frac{1 \text{ms}}{P} \right)^4 \text{ erg s}^{-1}. \quad \text{Spin-down power of a pulsar}$$

$$L = 4\pi n \gamma u_s^2 m_p c^3 (1 + \sigma), \quad (\gamma^2 = 1 + u^2), \quad \text{Wind luminosity is assumed to be comparable with the spin-down power}$$

$$\sigma = \frac{B^2}{4\pi n u \gamma m_p c^2},$$

Ratio of magnetic flux to the particle energy flux.

This is fixed by the outer boundary conditions.

$$\Delta\Phi = \frac{1}{2} \left(\frac{\Omega R}{c} \right)^2 R B_p$$

Electric potential difference between the pole and the feet of the corotating magnetosphere which is nearest to the pole.

$$\epsilon_{\text{max}} = 3 \times 10^{18} Z \left(\frac{B_p}{10^{12} \text{G}} \right) \left(\frac{1 \text{ms}}{P} \right)^2 \left(\frac{R}{10^6 \text{cm}} \right)^3 \text{ eV},$$

$$\gamma_{\text{max}} = 3.2 \times 10^9 \left(\frac{B_p}{10^{12} \text{G}} \right) \left(\frac{1 \text{ms}}{P} \right)^2 \left(\frac{R}{10^6 \text{cm}} \right)^3.$$

$$t_{\text{spin}} = 6.2 \times 10^9 \left(\frac{10^{12} \text{G}}{B_p} \right)^2 \left(\frac{10^6 \text{cm}}{R} \right)^6 \left(\frac{P}{1 \text{ms}} \right)^2 \text{ s}.$$

Maximum energy and bulk Lorentz factor of protons
Spin-down age

Hydrodynamics (2)

Shock Conditions

$$n_1 u_1 = n_2 u_2$$

$$E = \frac{u_1 B_1}{\gamma_1} = \frac{u_2 B_2}{\gamma_2}$$

$$\gamma_1 \mu_1 + \frac{EB_1}{4\pi n_1 u_1} = \gamma_2 \mu_2 + \frac{EB_2}{4\pi n_2 u_2}$$

$$\mu_1 u_1 + \frac{P_1}{n_1 u_1} + \frac{B_1^2}{8\pi n_1 u_1} = \mu_2 u_2 + \frac{P_2}{n_2 u_2} + \frac{B_2^2}{8\pi n_2 u_2}$$

Approximation (cold&relativistic)

$$\gamma_1 \sim u_1, P_1 \sim 0, \text{ and } \mu_1 \sim m_p c^2.$$



$$u_2^2 = \frac{8\sigma^2 + 10\sigma + 1}{16(\sigma + 1)} + \frac{1}{16(\sigma + 1)} [64\sigma^2(\sigma + 1)^2 + 20\sigma(\sigma + 1) + 1]^{1/2}.$$

$$\frac{P_2}{n_1 m_p c^2 u_1^2} = \frac{1}{4u_2 \gamma_2} \left[1 + \sigma \left(1 - \frac{\gamma_2}{u_2} \right) \right],$$

Relativistic Rankine-Hugoniot relations for perpendicular shock (μ : specific enthalpy)

Assumption: Relativistic Maxwellian



$$N(\gamma) = A\gamma \exp \left[-\frac{m_p c^2}{k_B T} (\gamma - 1) \right]$$

$$P_2 = \frac{2}{3} n_2 k_B T_2$$

Hydrodynamics (3)

Nebula Flow

Solution

$$\frac{d}{dr}(cnur^2) = 0;$$

$$(1 + u_2^2 v^2)^{1/2} \left[\delta + \Delta (vz^2)^{-1/3} + \frac{1}{v} \right] = \gamma_2 (1 + \delta + \Delta),$$

Conservation of number flux

$$\frac{d}{dr} \left(\frac{ruB}{\gamma} \right) = 0;$$

v is defined as $v = u/u_2$, z is defined as $z = r/r_s$, δ is defined as $\delta = 4\pi n_2 \gamma_2^2 m_p c^2 / B_2^2$

$$\Delta = 16\pi P_2^2 \gamma_2^2 B_2^2$$

$$P_T = P + \frac{E^2 + B^2}{8\pi} = \frac{L}{4\pi r_s^2 c (1 + \sigma)} \left[\frac{P_2}{n_1 m_p c^2 u_1^2} (vz^2)^{-4/3} + \frac{\sigma}{z^2} \left(1 + \frac{1}{2u_2^2 v^2} \right) \right]$$

Conservation of magnetic flux

$$\frac{d}{dr} (ur^2 e) + P \frac{d}{dr} (r^2 u) = 0;$$

Functions of σ and r



Propagation of thermal energy

In particular,

$$u_\infty = \left(\frac{\sigma^2}{1 + 2\sigma} \right)^{1/2}$$

Location of the termination shock and value

of σ are **determined** so as to achieve a contact discontinuity at the outer boundary.

Conservation of total energy

$$\frac{d}{dr} \left[nur^2 \left(\gamma\mu + \frac{B^2}{4\pi n\gamma} \right) \right] = 0;$$

Hydrodynamics (4)

Outer boundary conditions (interface between nebula flow and supernova ejecta)

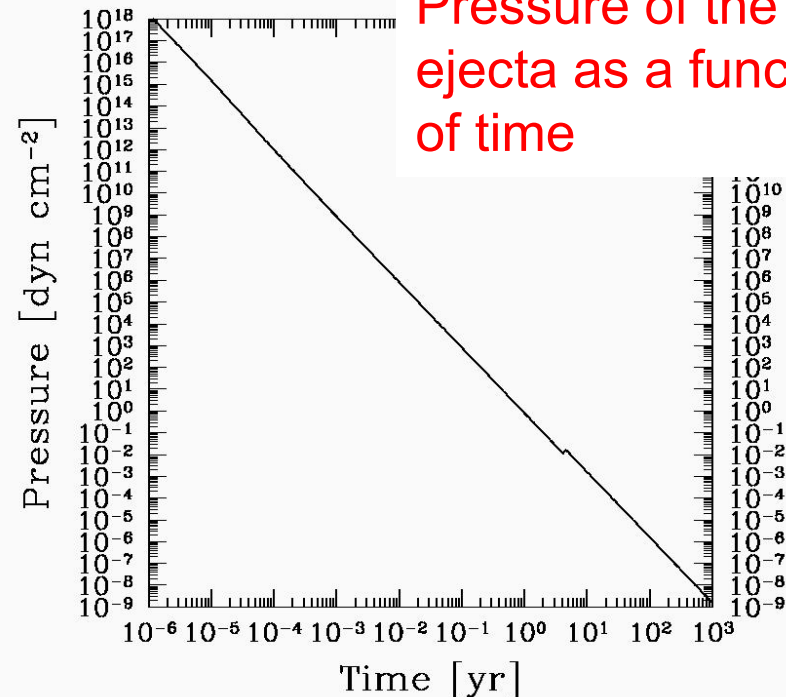
Contact discontinuity

$$V_{\text{Nebula}} = V_{\text{SNR}} = 2000 \text{ km/s}$$

$$P_{\text{Nebula}} = P_{\text{SNR}}$$

$$\sigma = 0.0067$$

Pressure of the SN ejecta as a function of time



$$\begin{aligned} E_{\text{th}} &= 0.02 \times 10^{51} \times \frac{6M_{\odot}}{20M_{\odot}} \text{ erg} \\ &= 6 \times 10^{48} \text{ erg,} \end{aligned}$$

Thermal energy in a He layer

$$E_{\text{th}} = \frac{3}{2}(N_e + N_{\text{He}})k_B T + 3aT^4 V$$

$$V = \frac{4}{3}\pi [V_{\text{max}}^3 - V_{\text{min}}^3] \left(\frac{t}{1\text{sec}}\right)^3,$$

Volume of the remnant

$V_{\text{max}} = 3000 \text{ km/s}$, $V_{\text{min}} = 2000 \text{ km/s}$

$$P = (n_e + n_{\text{He}})k_B T + aT^4,$$

Microphysics of Proton-Proton Interaction (1)

Fluid rest frame \longrightarrow Observer's frame

$$dR_{12} = \sigma_{pp} v_{\text{rel}} \frac{p_1}{E_1} \frac{p_2}{E_2} n_1 n_2 dV dt$$

$$= c \sigma_{pp} n_1 n_2 \sqrt{(\vec{\beta}_1 - \vec{\beta}_2)^2 - (\vec{\beta}_1 \times \vec{\beta}_2)^2} dV dt,$$

$$\frac{dF'(E'_\pi)}{d\Omega'} = \frac{1}{\Gamma'^2 (1 - \beta' \cos \theta')^2} \frac{F(E_\pi)}{4\pi},$$

$$E'_\pi = \frac{1}{\Gamma' (1 - \beta' \cos \theta')} E_\pi.$$

Number of collisions that occur in a volume dV , for a time dt with monotonic spectrums in the momentum space.

$$\frac{F(E_\pi)}{dV} = c \int_1^\infty d\gamma_2 \int_1^{\gamma_2} d\gamma_1 \int_{-1}^1 d\cos\theta \frac{d\sigma_{pp}(\gamma_1, \gamma_2, \cos\theta)}{dE_\pi} n(R, \gamma_1) n(R, \gamma_2)$$

$$\times \sqrt{(\vec{\beta}_1 - \vec{\beta}_2)^2 - (\vec{\beta}_1 \times \vec{\beta}_2)^2},$$

However, the bulk flow is non-relativistic in the nebula flow. Thus, number spectrum is not so deformed due to this Lorenz transformation.

Number spectrum of pions [particles cm⁻³ s⁻¹ erg⁻¹]

$$\cos \theta = \frac{\vec{\beta}_1 \cdot \vec{\beta}_2}{|\vec{\beta}_1| |\vec{\beta}_2|}$$

$d\sigma_{pp}(\gamma_1, \gamma_2, \cos \theta) / dE_\pi$ Differential cross section

$$\frac{dF(E_\pi)}{d\Omega} = \frac{1}{4\pi} \int_{\Delta V} \frac{F(E_\pi)}{dV} dV, \quad \Delta V \text{ is the fluid element}$$

Number spectrum of pions is unit solid angle [particles cm⁻³ s⁻¹ erg⁻¹ sr⁻¹]

Relativistic Maxwellian

Microphysics of Proton-Proton Interaction (2)

Calculation of the differential cross section $d\sigma_{pp}(\gamma_1, \gamma_2, \cos \theta) / dE_\pi$

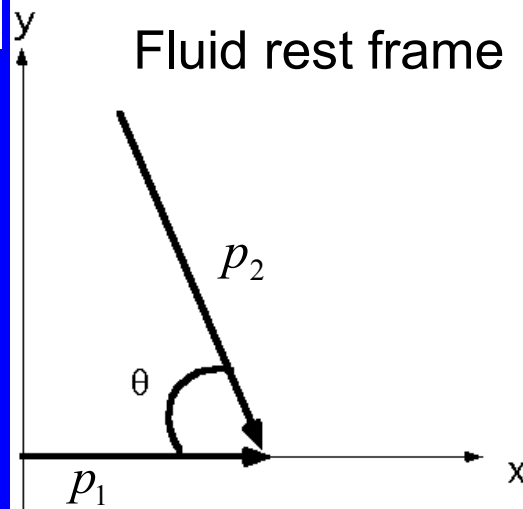
Procedure: Fluid rest \longrightarrow Particle1 rest \longrightarrow Fluid rest

$$p'_\pi = \begin{pmatrix} \sqrt{p_\pi'^2 + m_\pi^2 c^2} \\ p'_\pi \{ \cos \alpha' \cos \theta' - \sin \alpha' \cos \phi' \sin \theta' \} \\ -p'_\pi \{ \cos \alpha' \sin \theta' + \sin \alpha' \cos \phi' \cos \theta' \} \\ p'_\pi \sin \alpha' \sin \phi' \end{pmatrix}$$

Four momentum of a pion in the Lab frame

$$\begin{pmatrix} \gamma_1 & \gamma_1 \beta_1 & 0 & 0 \\ \gamma_1 \beta_1 & \gamma_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} p'_\pi = \begin{pmatrix} \gamma_1 \sqrt{p_\pi'^2 + m_\pi^2 c^2} + \gamma_1 \beta_1 p'_\pi \{ \cos \alpha' \cos \theta' - \sin \alpha' \cos \phi' \sin \theta' \} \\ \gamma_1 \beta_1 \sqrt{p_\pi'^2 + m_\pi^2 c^2} + \gamma_1 p'_\pi \{ \cos \alpha' \cos \theta' - \sin \alpha' \cos \phi' \sin \theta' \} \\ -p'_\pi \{ \cos \alpha' \sin \theta' + \sin \alpha' \cos \phi' \cos \theta' \} \\ p'_\pi \sin \alpha' \sin \phi' \end{pmatrix}$$

Fluid rest frame

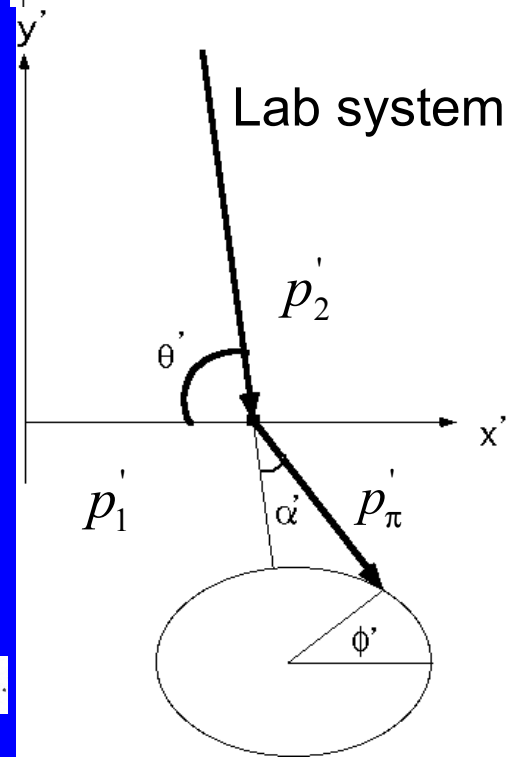


Since

$$\int dE_\pi \frac{d\sigma_{pp}(\gamma_1, \gamma_2, \cos \theta)}{dE_\pi} = \int dE'_\pi \frac{d\sigma_{pp}(E'_\pi, E'_2)}{dE'_\pi}$$

Result:

$$\frac{d\sigma_{pp}(\gamma_1, \gamma_2, \cos \theta)}{dE_\pi} = \frac{d}{dE_\pi} \int \int \int dE'_\pi d\phi' d\cos \alpha' \sqrt{E_\pi'^2 - m_\pi^2 c^4} \left(E'_\pi \frac{d^3 \sigma_{pp}}{dp_\pi'^3 c^3} \right) \times H(\gamma_1 \sqrt{p_\pi'^2 + m_\pi^2 c^2} + \gamma_1 \beta_1 p'_\pi \{ \cos \alpha' \cos \theta' - \sin \alpha' \cos \phi' \sin \theta' \} - E_\pi) \times H(E_\pi + dE_\pi - \gamma_1 \sqrt{p_\pi'^2 + m_\pi^2 c^2} + \gamma_1 \beta_1 p'_\pi \{ \cos \alpha' \cos \theta' - \sin \alpha' \cos \phi' \sin \theta' \})$$



Where

$$\tilde{x} = \{ x_\parallel^{*2} + (4/s)(p_\perp^{*2} c^2 + m_p^2 c^4) \}^{1/2}$$

$$E_\pi^* \frac{d^3 \sigma_\pi^*}{d^3 p_\pi^*} = \frac{A}{(1 + 4m_p^2 c^4 / s)^r} (1 - \tilde{x})^q \exp \left[\frac{B p_\perp^*}{1 + 4m_p^2 c^4 / s} \right]$$

$$x_\parallel^* = p_\parallel^* c / \sqrt{s/4 - m_p^2 c^4}$$

$$q = (C_1 + C_2 p_\perp^* + C_3 p_\perp^*)$$

Scaling law model (Badhwar et al. 1977)

§ Results

In this study, we have to check whether the energy spectrum of protons can be regarded to obey the Maxwellian distribution.

—————> From this argument, some constraints are derived.

- (i) Production rate of pions [erg/s] should be much smaller than the luminosity of the pulsar wind.
- (ii) Synchrotron cooling timescale of protons should be longer than dynamical timescale and/or pp collision timescale.
- (iii) Energy transfer timescale from protons to electrons should be longer than dynamical timescale and/or pp collision timescale.

$$t_{p,\text{syn}} = \left(\frac{m_p}{m_e}\right)^4 \times t_{e,\text{syn}} \sim 1.1 \times 10^{13} t_{e,\text{syn}},$$

$$t_{\text{travel}} = \frac{r}{v},$$

$$t_{\text{ep}} = \frac{4}{\ln \Lambda} \frac{n_e}{n_p} \left(\frac{kT_e}{m_e c^2}\right)^2 \frac{1}{n_e \sigma_{TC}}$$

$$t_{e,\text{syn}} = 3.9 \times 10 (1 \text{ GeV}/E) (10^2 \text{ G}/B)^2 \text{ s.}$$

$$t_{\text{col}} = \frac{1}{n \sigma_{pp} c},$$

$$\ln \Lambda = \ln \left[\frac{kT_e}{\hbar \omega_p} \right]$$

$$\omega_p = \left(\frac{4\pi e^2 c^2 n_e}{3kT_e} \right)^{1/2}$$

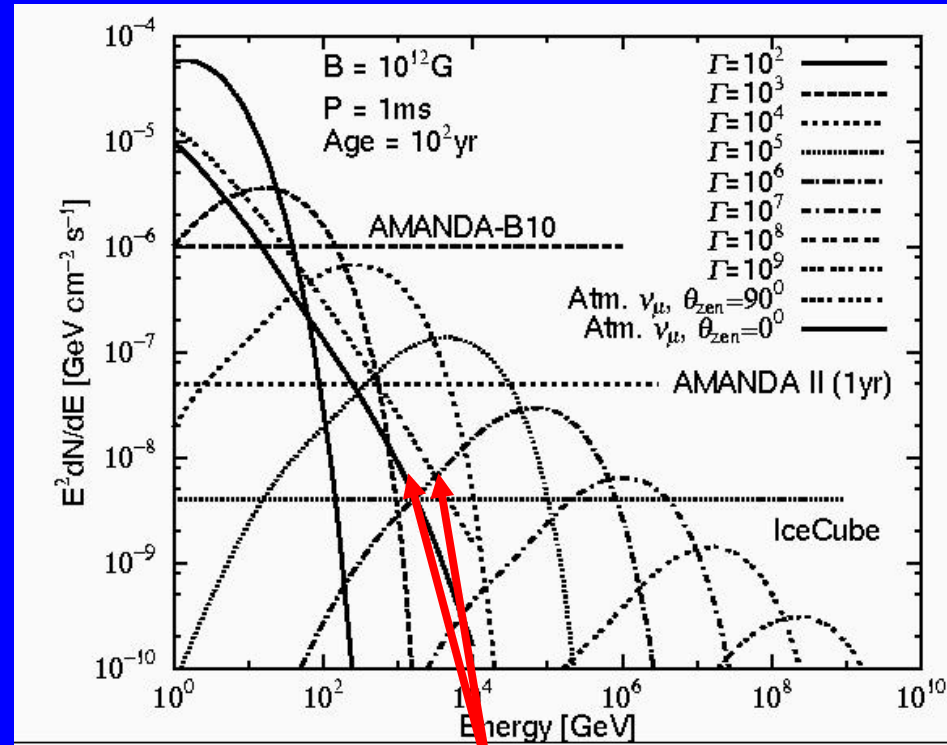
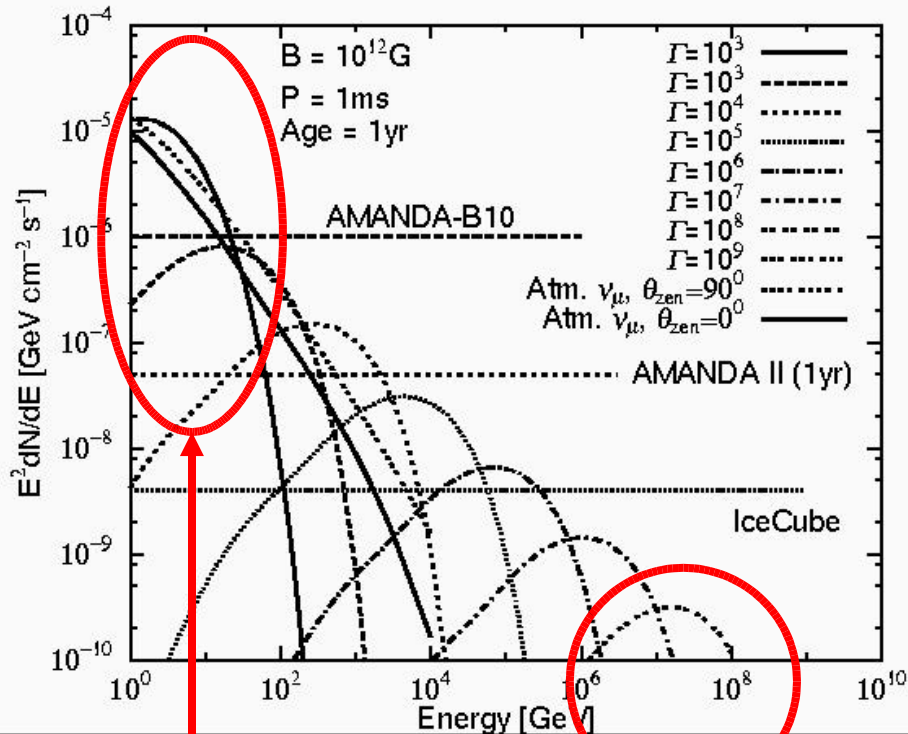
(t_{ad} , t_{μ} , t_{sync} , t_{ic}) : Later

Spectrum of Energy Fluxes of Neutrinos from a Pulsar

Age=1yr

D=10kpc

Age=100yr



Low energy (T:small)
High flux (n:large)

High energy (T:large)
Low flux (n:small)

Atmospheric
neutrino

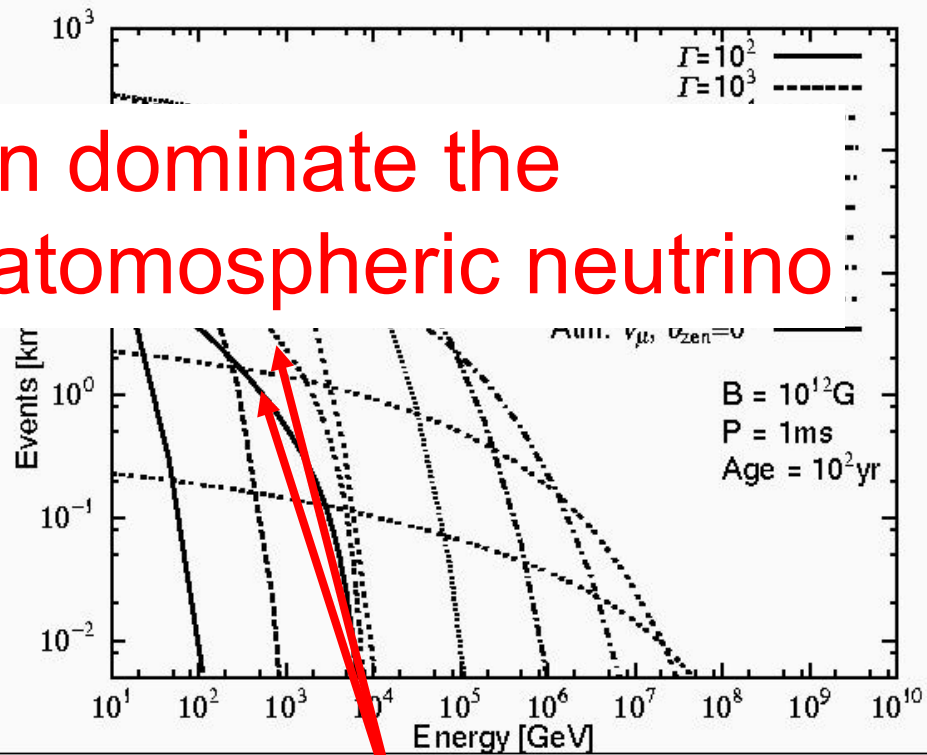
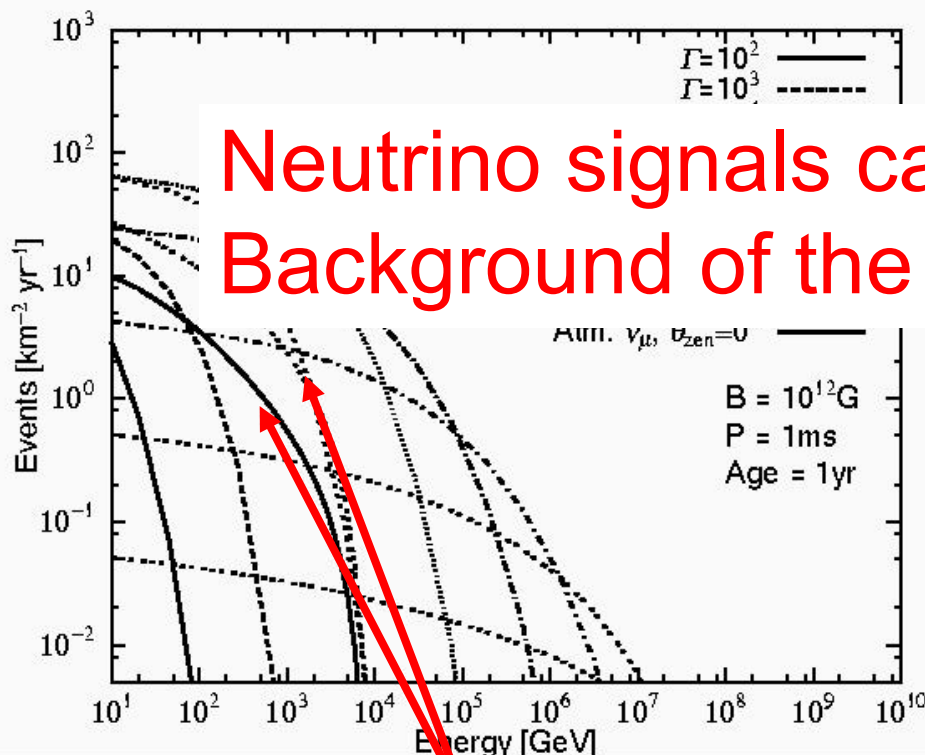
Neutrino Event Rate per Year from a Pulsar as a Function of Muon Energy Threshold

Age=1yr

D=10kpc

Age=100yr

Neutrino signals can dominate the Background of the atmospheric neutrino



Atmospheric neutrino

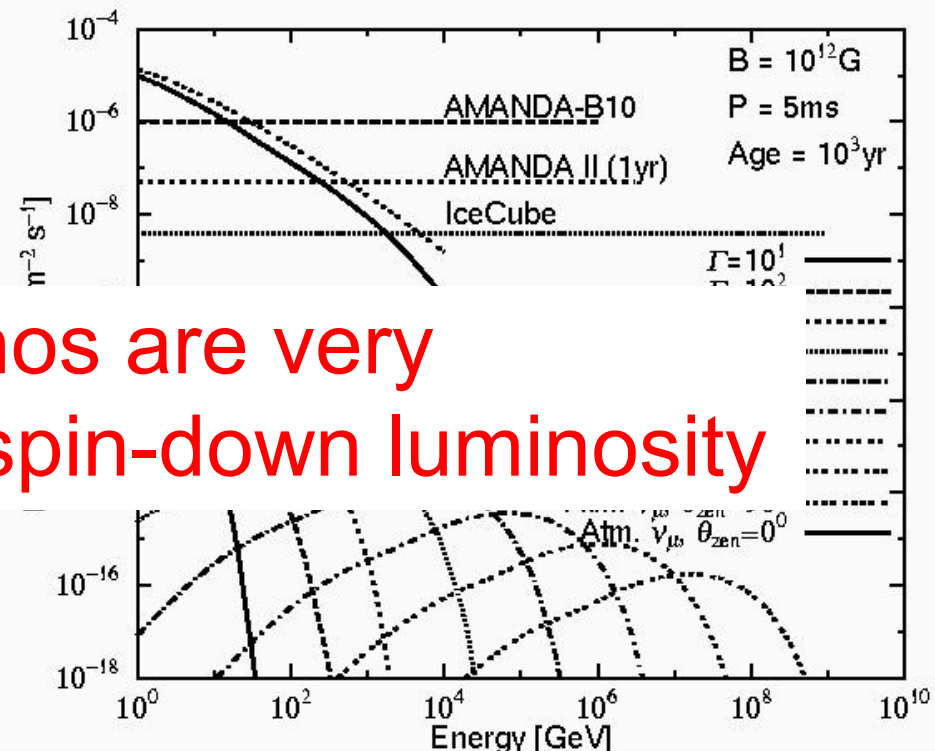
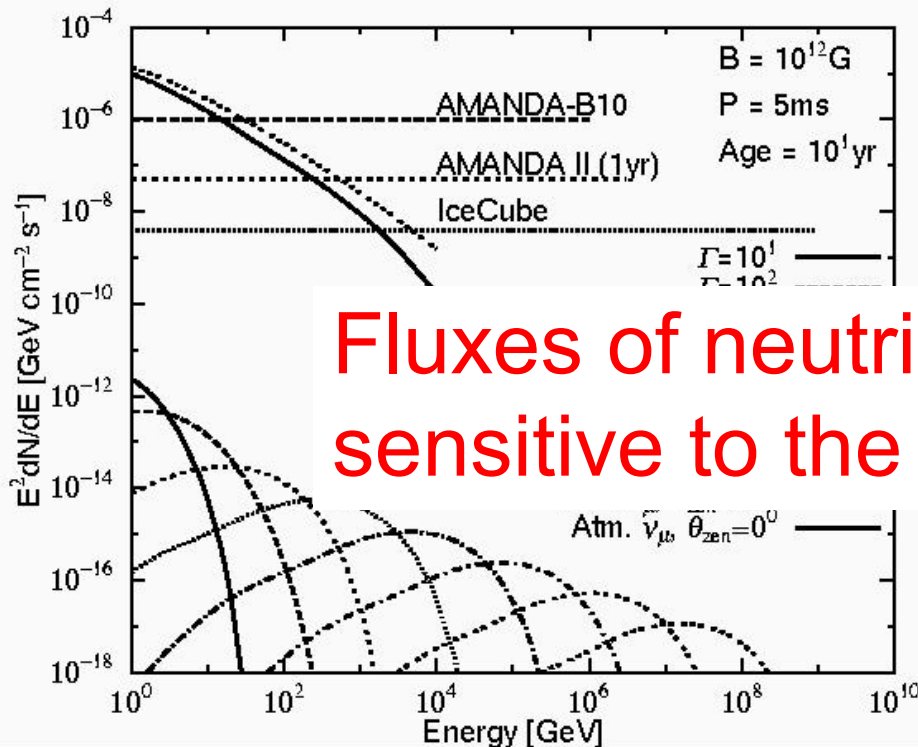
Atmospheric neutrino

Spectrum of Energy Fluxes of Neutrinos from a Pulsar with $P=5\text{ms}$

Age=10yr

$D=10\text{kpc}$

Age=1000yr



Fluxes of neutrinos are very sensitive to the spin-down luminosity

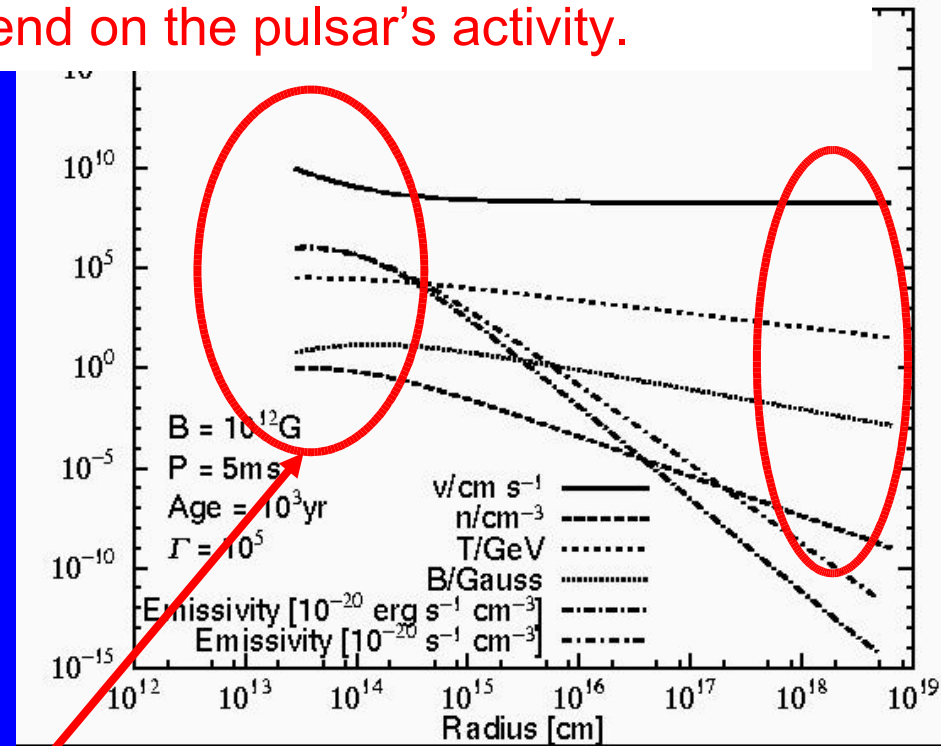
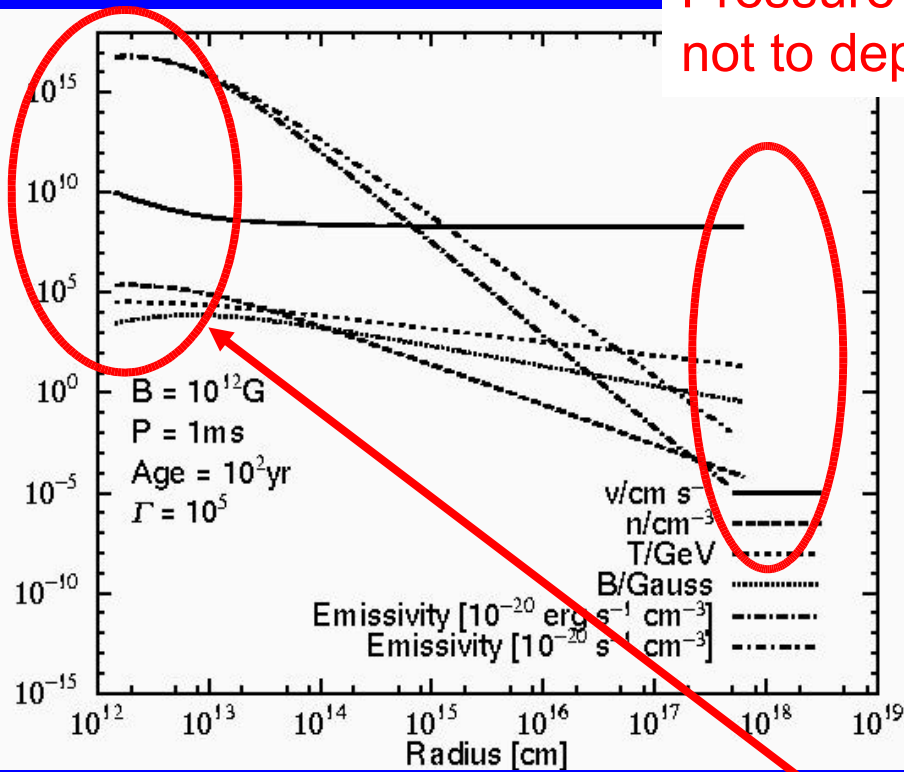
Fluxes of neutrinos are too low to be detected in the cases where $B=10^{12}\text{G}$ and $P=5\text{ms}$.

Profiles of Velocity, Number Density, Temperature, Magnetic Field, and Emissivity of Charged Pions for a Pulsar with $P=5\text{ms}$

$P=1\text{ms}$

$P=5\text{ms}$

Pressure of the supernova ejecta is assumed not to depend on the pulsar's activity.



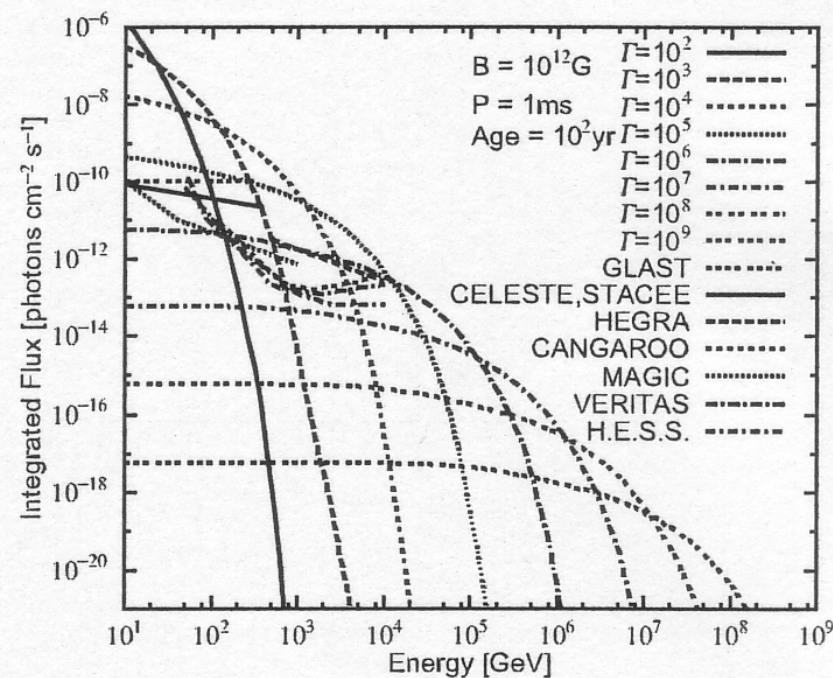
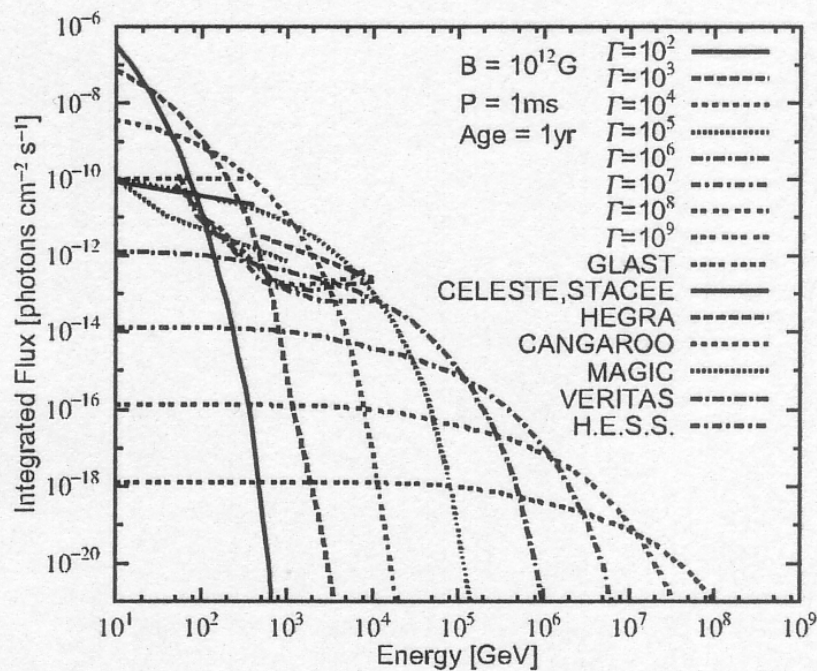
$P(\text{period}) \searrow$
 $L \nearrow$
 $r_s \searrow$
 $n \nearrow$
 $\epsilon \nearrow$

Integrated Gamma-ray Fluxes from Neutral Pion Decays

Age=1yr

P=1ms, D=10kpc

Age=100yr



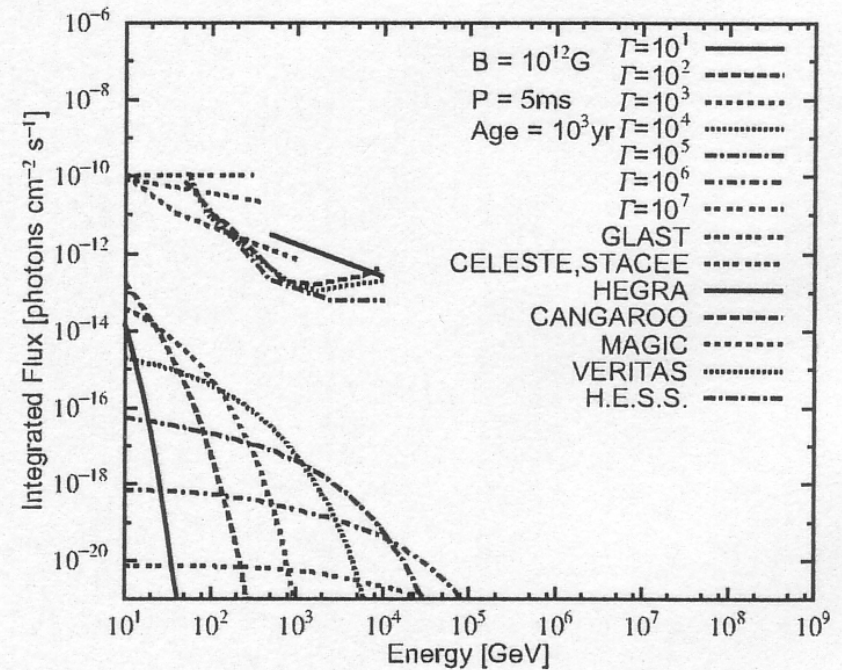
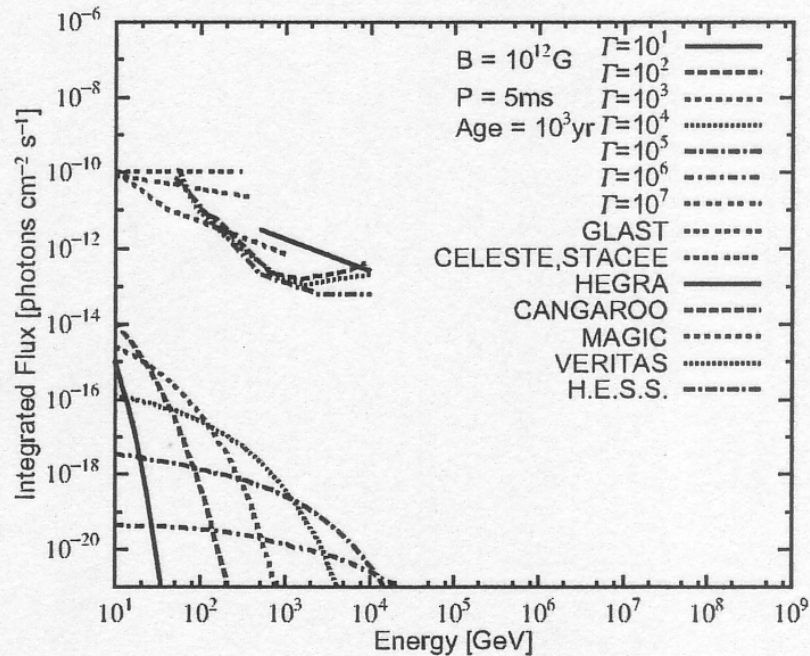
Gamma-rays will be detected by Cherenkov Detectors as well as gamma-ray satellites.

Integrated Gamma-ray Fluxes from Neutral Pion Decays from a Pulsar with $P=5\text{ms}$

Age=10yr

$D=10\text{kpc}$

Age=1000yr



Fluxes of gamma-rays are too low to be detected in the cases where $B=10^{12}\text{G}$ and $P=5\text{ms}$.

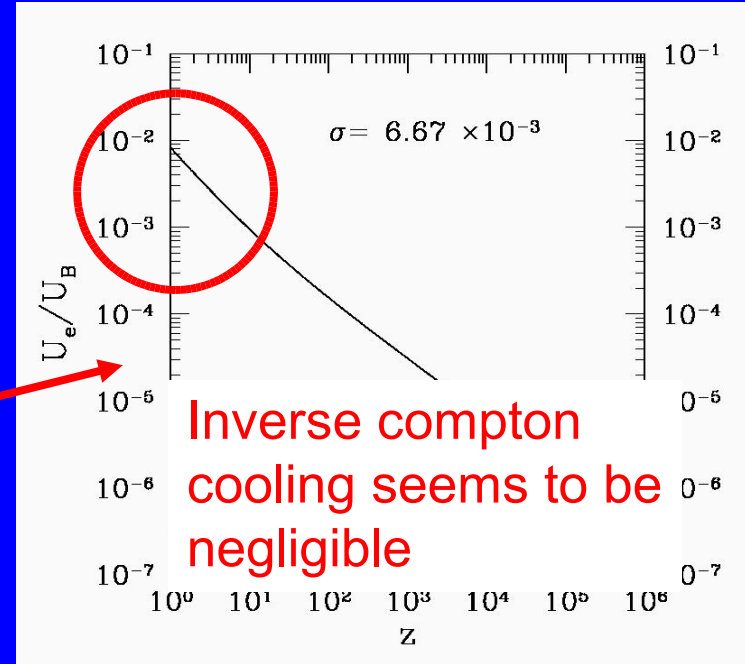
§ Discussions

Other timescales

1. Inverse compton cooling timescale

$$\frac{t_{\text{sync}}}{t_{\text{IC}}} = \frac{U_\gamma}{U_B},$$

$$\frac{t_{\text{sync}}}{t_{\text{IC}}} \leq \frac{U_e}{U_B} = \frac{m_e U_p}{m_p U_B} = \frac{m_e}{m_p} \frac{z^2 \{3\sigma + (3\sigma/z)^{2/3}\}^2}{\sigma \{3\sigma z^2 + (3\sigma)^{2/3} z^{4/3}\}^{4/3} [4 + \{3\sigma + (3\sigma/z)^{2/3}\}^2]}.$$



2. Synchrotron cooling timescale of muon

$$\begin{aligned} t_{\mu, \text{syn}} &= \left(\frac{m_\mu}{m_e}\right)^4 \times t_{e, \text{syn}} \sim 1.82 \times 10^9 t_{e, \text{syn}} \\ &= 7.11 \times 10^{10} (1 \text{ GeV}/E_\mu) (10^2 \text{ G}/B)^2 \text{ s}. \end{aligned}$$

When $E_\mu \geq 5.85 \times 10^5 \left(\frac{10^4 \text{ G}}{B}\right) \text{ GeV},$

mean lifetime of muon becomes longer than the synchrotron cooling time.

3. Adiabatic cooling time is taken into consideration by adopting nebula flow equations.

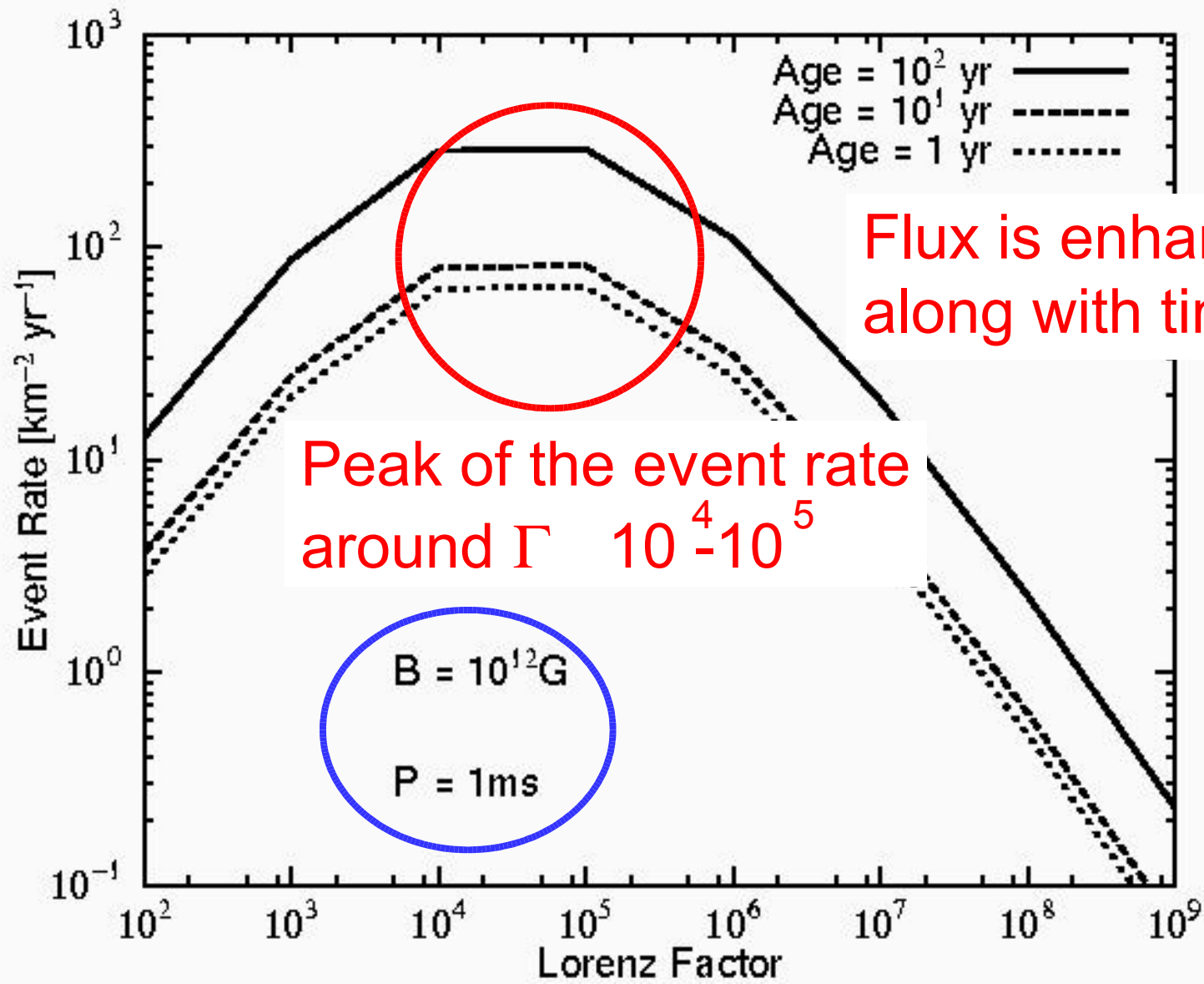
§ Conclusion

We have estimated fluxes of neutrinos and gamma-rays from a pulsar surrounded by supernova ejecta in our galaxy, including an effect that has not been taken into consideration, that is, **interactions between high energy cosmic rays themselves** in the nebula flow.

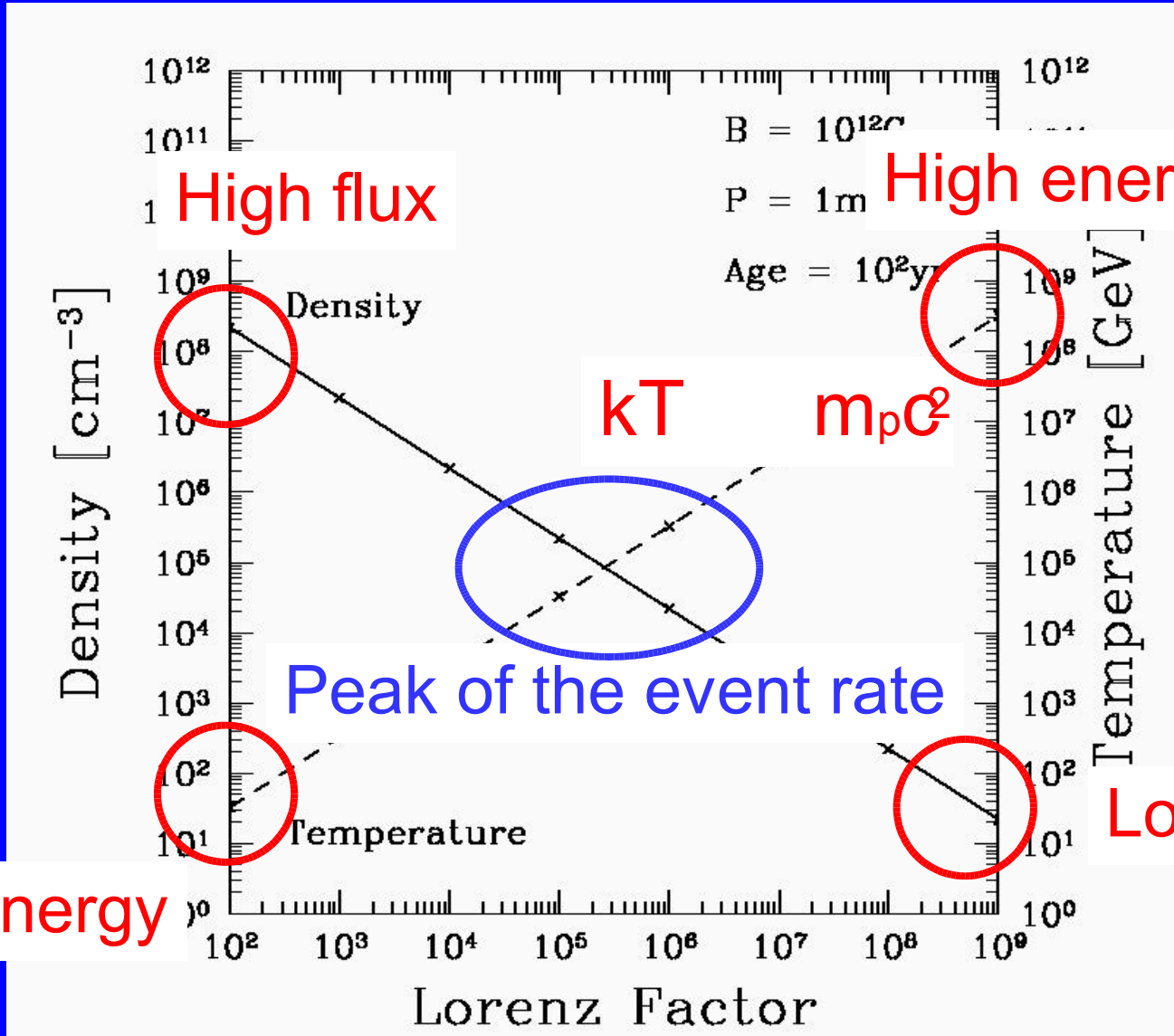
We have found that fluxes of neutrinos and gamma-rays depend very sensitively on the wind luminosity. In the case where $B=10^{12}$ G and $P=1$ ms, neutrinos should be detected by km^2 high energy neutrino detectors such as AMANDA, ANTARES, and IceCube. Also, gamma-rays should be detected by Cherenkov telescopes such as Cangaroo, MAGIC, VERITAS, and HESS as well as by GLAST satellite.

We have found that interactions between high energy cosmic rays themselves are so effective that this effect can be confirmed by future observations. Thus, we conclude that it is worth while investigating this effect further in the near future.

Event Rates of Neutrino whose energy is greater than 10GeV



Density and Temperature behind the Termination Shock



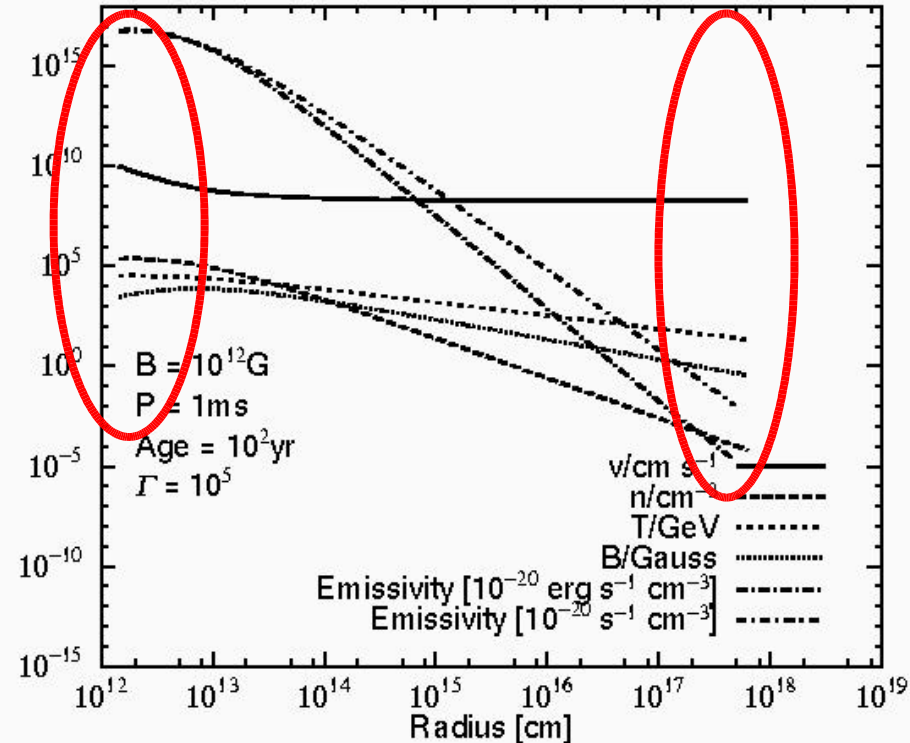
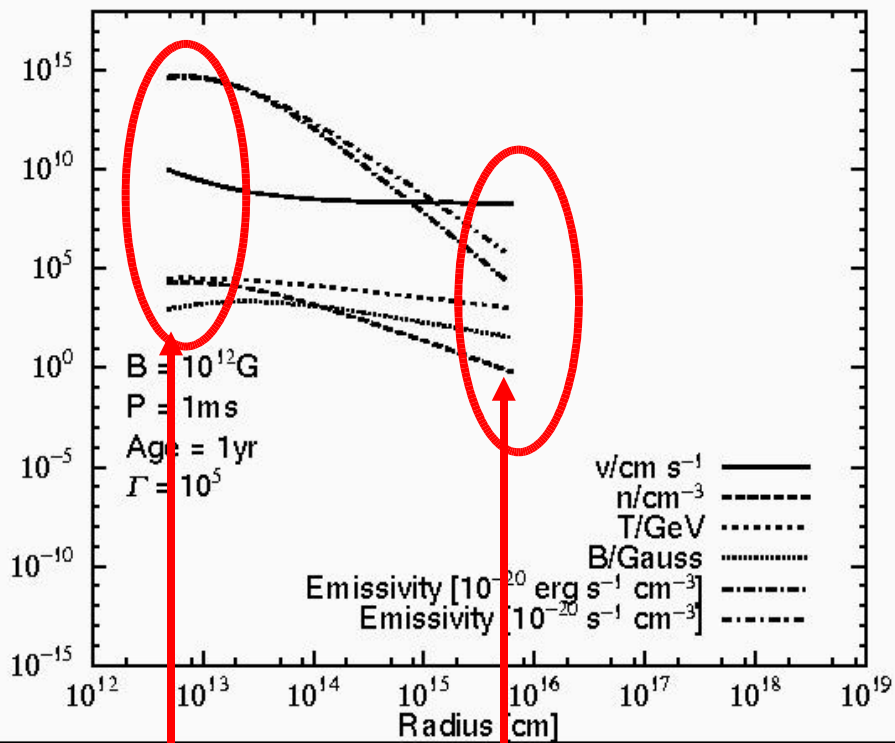
Profiles of velocity, Number Density, Temperature, Magnetic Field, and Emissivity of Charged Pions

Age=1yr

Location of the Termination shock moves inwardly

Age=100yr

Pressure is lower



Location of the Termination shock

Inner-edge of the supernova ejecta

Emissivity \uparrow $P \searrow$ $r \searrow$ $n \nearrow$ $F \nearrow$

$$\epsilon = n^2 c \sigma_{pp} = 3 \times 10^{-5} \left(\frac{n}{10^5 \text{ cm}^{-3}} \right) \left(\frac{\sigma_{pp}}{100 \text{ mb}} \right)$$